

UNIVERSIDAD DE LOS ANDES		DEPARTAMENTO DE MATEMATICAS	
PROGRAMA DEL CURSO RSO 01112 Y 01164			
II SEMESTRE DE 1997			
TEXTO: Cálculo con Geometría Analítica, E. J. Purcell, D. Varberg.			
Fotocopias: Complejos, polinomios, Suplemento.			
No.	Fecha	Teoría	Problemas
1	Agost 11-Lu	Inducción	
2	12 Ma	Introducción	
3	13 Mi	7.1	9,11,13,14,15,18,20,25,30
4	14 Ju	7.1	38,39,40,43,45,47,49
5	15 Vi	7.2	7,13,26,27,35,41
	18 Lu-Fiesta		
6	19 Ma	7.3	3,7,10,17,21,22,25
7	20 Mi	7.4	7.3: 29,32,34,38,39,45
8	21 Ju	7.5	7,4:3,6,15,18,20,27,33,42,43,44
9	22 Vi	7.5	8,15,24,26,27
10	25 Lu	7.6 - 7.7	7.6: 33,35,36; 7.7: 8,13
11	26 Ma	7.7	22,27,47,49,50
12	27 Mi	7.8 - 7.9	7.8: 4,14,23,29; 1,15
13	28 Ju	7.9	7.9: 16,30, pd: 27,28,33,41
14	29 Vi	Suplemento 0,1,2	
15	Sept. 1 Lu	Suplemento 0,1,2	
16	2 Ma	I Parcial	
17	3 Mi	Complejos	
18	4 Ju	Complejos	
19	5 Vi	Complejos	
20	8 Lu	Complejos - Polinomios	
21	9 Ma	Polinomios	
22	10 Mi	Polinomios	
23	11 ju	Suplemento 3,4,5	
24	12 Vi	8.1	7,8,9,12,15,23
25	15 lu	8.1	24,26,29,51,71,72
26	16 Ma	8.2	1,2,3,4,10,11,12,22,26
27	17 Mi	8.3	3,18,20,23,26,30
28	18 Ju	8.4	5,7,11,12,15,18,21,23
29	19 Vi	8.5	3,9,10,13,21,25; 8.6: 1-25
30	22 Lu	Suplemento 6,7,8,9,10,11,12,13	24 al 29:86 pd 16,42,45,46
31	23 Ma	Suplemento 6,7,8,9,10,11,12,13	24 al 29 :86 pd 16,42,45,46
32	24 Mi	Suplemento 6,7,8,9,10,11,12,13	24 al 29 :86 pd 16,42,45,46
33	25 Ju	II Parcial	
34	26 Vi	18.1	1,5,7,12,15
RECESO : SEPT.29 - OCT.4			
6 Lu - Ultimo día de retiros			
35	6 Lu	18.1	17,18,19,21
36	7 Ma	18.2	3,5,9,11,13,14,15
37	8 Mi	18.3	3,5,17,20
38	9 Ju	18.4	1,5,11,14,15
39	10 Vi	18.5	1 al 9: pd 2,6,15,18,20,23
	13 Lu - Fiesta		
40	14 Ma	9.1	6,16,18,23,26
41	15 Mi	9.2	18,21,23,31,32,33,40,41
42	16 Ju	9.3	3,5,7,9,19,25,28,36
43	17 Vi	9.4	2,5,15,26,27,28,29,30,31

44	20 Lu	9.5	1,25
45	21 Ma	Suplemento 14,15	50 AL 63
46	22 Mi	Suplemento 14,15	50 al 63
47	23 Ju	III Parcial	
48	24 Vi	10.1	15,18,21,23,31
49	27 Lu	10.2	17,18,24
50	28 Ma	11.1	1,3,5,7,9,17,18,23
51	29 Mi	11.2	11.1: 30,34,48,49,50,51; 11.2: 2,35,7
52	30 Ju	11.2	11.2:10,11,13,25,29,30,45
53	31 Vi	11.3	11.3: 1,3,5,7,9
Nov .3 Lu Fiesta			
54	4 Ma	11.3	11.3: 15,29,30,31
55	5 Mi	6.1-6.2 (Matemáticas Financiera)	
56	6 Ju	6.3-6.4 (Matemáticas Financiera)	
57	7 Vi	6.5	
58	10 Lu	11.4	11.4: 1,2,3,4,7,9
59	11 Ma	11.4	11.4: 13,16,17,19,23,36,37
60	12 Mi	11.5	11.5: 13 al 20
61	13 Ju	11.5-11.6	11.5:39,41; 11.6: 1,5,9
62	14 Vi	11.7	11.6: 15,17,27,11.7: 1 al 10
17 Lu-Fiesta			
63	18 Ma	11.8	11.7: 17 al 24 ; 11.8 : 1 al 16
64	19 Mi	12.1	5,7,13,14,29,30,31
65	20 Ju	12.2- 12.3	12.2: 5,7,8,9,16,21,25,38,41
66	21 Vi	12.3 - 12.4	12.3: 4,9,13,18,22,28,12.4 : 7,14,19,36,46
67	24 Lu	12.6	5,10,16,21,31,35,40
68	25 Ma	12.7	7,12,17,21,29,31,35,41
69	26 Mi	12.8	9,16,20,22,23,24,26,27
70	27 Ju	IV Parcial	
71	28 Vi	Repaso	
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Exámenes parciales, interrogatorios orales, tablero, quices, etc.			
examen final : 25 % Total : 100%			
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